

Unit 5 Test Review

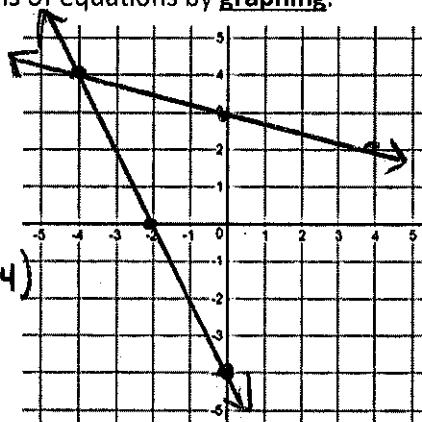
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Solve the following systems of equations by graphing.

$$1. \begin{aligned} 2x + y &= -4 \\ x + 4y &= 12 \end{aligned}$$

$$\begin{aligned} -x & \\ -x & \end{aligned}$$

$$\begin{aligned} 4y &= -x + 12 \\ \frac{4y}{4} &= \frac{-x}{4} + \frac{12}{4} \\ y &= -\frac{1}{4}x + 3 \end{aligned}$$



Check your solution: $(-4, 4)$

$$2(-4) + 4 = -4$$

$$\begin{aligned} -8 + 4 &= -4 \\ -4 &= -4 \quad \checkmark \end{aligned}$$

$$-4 + 4(4) = 12$$

$$-4 + 16 = 12$$

$$12 = 12 \quad \checkmark$$

$$2. \begin{aligned} y &= 3x + 3 \\ y &= x^2 + 3x + 2 \end{aligned}$$

$$x \mid y$$

$$1 \mid 6$$

$$-1 \mid 0$$

$$-2 \mid 0$$

$$-1.5 \mid -0.25$$

Check your solution:

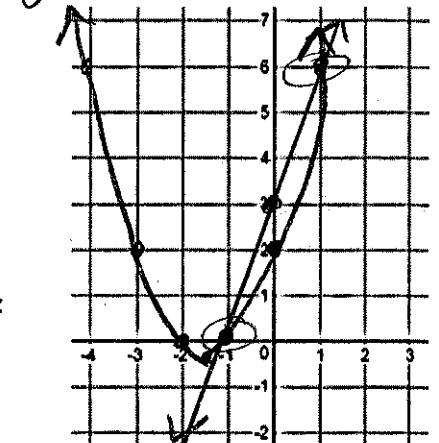
$$(1, 6) (-1, 0)$$

$$6 = 3(1) + 3$$

$$6 = 6 \quad \checkmark$$

$$6 = 1^2 + 3(1) + 2$$

$$6 = 6 \quad \checkmark$$



$$0 = 3(1) + 3$$

$$0 = 0 \quad \checkmark$$

$$0 = (-1)^2 + 3(-1) + 2$$

$$0 = 1 - 3 + 2$$

$$0 = 0 \quad \checkmark$$

3. Explain in words: How can you find a solution to a system of equations from a graph?

The solution can be seen in the intersection(s) of the graphs of the functions.

4. Solve the following system using the substitution method: $y = 2x - 10$
 $y = 4x - 8$

$$\begin{aligned} 2x - 10 &= 4x - 8 \\ -4x &+ 10 = 4x - 8 \\ -2x &= 2 \\ x &= -1 \\ 4 &= 2(-1) - 10 \\ &= -2 - 10 \\ &= -12 \end{aligned} \quad (-1, -12)$$

5. Solve the following system using the elimination method: $\begin{cases} 8x + 3y = 13 \\ 3x + 2y = 11 \end{cases}$

$$\begin{aligned} 3(-1) + 2y &= 11 \\ -3 + 2y &= 11 \\ +3 & \\ 2y &= 14 \\ \frac{2y}{2} &= \frac{14}{2} \\ y &= 7 \end{aligned}$$

$$\begin{aligned} 8x + 3y &= 13 \\ 3x + 2y &= 11 \end{aligned} \rightarrow \begin{aligned} 16x + 6y &= 26 \\ -9x - 6y &= -33 \\ \hline 7x &= -7 \\ \frac{7x}{7} &= \frac{-7}{7} \\ x &= -1 \end{aligned}$$

$$\begin{aligned} y &= 10^2 - 81 \\ &= 100 - 81 \\ &= 19 \end{aligned} \quad \begin{aligned} y &= 8^2 - 81 \\ &= 64 - 81 \\ &= -17 \end{aligned}$$

$$6. \text{ Solve the following system } \underline{\text{algebraically}}: \begin{aligned} y &= x^2 - 81 \\ y &= 18x - 161 \end{aligned}$$

$$\begin{aligned} x^2 - 81 &= 18x - 161 \\ -18x + 161 &= -18x + 161 \end{aligned}$$

$$\begin{aligned} (10, 19) \\ (8, -17) \end{aligned}$$

$$x = \frac{+18 \pm \sqrt{(-18)^2 - 4 \cdot 1 \cdot 80}}{2 \cdot 1}$$

$$= \frac{18 \pm \sqrt{324 - 320}}{2}$$

$$= \frac{18 \pm \sqrt{4}}{2}$$

$$\frac{18+2}{2} = \frac{20}{2} = 10$$

$$\frac{18-2}{2} = \frac{16}{2} = 8$$

$$\begin{aligned} x^2 - 18x + 80 &= 0 \rightarrow a = 1 \\ (x - 10)(x - 8) &= 0 \quad b = -18 \\ x - 10 &= 0 \quad c = 80 \\ x &= 10 \quad x - 8 = 0 \\ x &= 8 \end{aligned}$$

7. Fill out the table for each of the following equations below:

a. $y = 6x - 11$

x	y
-3	-29
-2	-23
-1	-17
0	-11
1	-5
2	1
3	7

b. $2x + 3y = 7$

x	y
-3	$4\frac{1}{3}$
-2	$3\frac{2}{3}$
-1	3
0	$2\frac{1}{3}$
1	$1\frac{2}{3}$
2	1
3	$\frac{1}{3}$

b. Use the tables to find the solution to the system of equations:

$$y = 6x - 11$$

$$2x + 3y = 7$$

$$-2x \quad -2x$$

$$\frac{3y}{3} = \frac{-2x+7}{3} \quad y = -\frac{2}{3}x + \frac{7}{3}$$

(2, 1)

c. Explain in words how you used the table to find your answer in part b.

I saw where the tables gave identical x and y values

9. Kona coffee sells for \$51 per pound and Colombian coffee sells for \$11 per pound. Sylvia wants to mix these two types of coffee to create 100 pounds of Breakfast Blend coffee that will sell for \$25 per pound.

a. How much would the 100 pound mix cost?

$$\$25 \times 100 = 2500$$

b. Write a system of equations that would describe this situation.

$$k + c = 100$$

$$51k + 11c = 2500$$

c. Solve the system algebraically (substitution or elimination).

$$k = 100 - c$$

$$51(100 - c) + 11c = 2500$$

$$5100 - 51c + 11c = 2500$$

$$-5100$$

$$-40c = 2600$$

$$c = 65$$

$$k + 65 = 100$$

$$-65 \quad -65$$

$$k = 35$$

65lb of Colombian
35lb of Kona

8. A metallurgist (someone who mixes metals) needs to make 50 pounds of an alloy (metal mixture) containing 50% gold.

He is going to melt and combine one metal that is 20% gold with another metal that is 70% gold. How much of each should he use?

a. How much would the 100 pound mix cost?
How many pounds of gold would

$$50 \times (0.5) = 25 \text{ lb}$$

b. Write a system of equations that would describe this situation.

$$0.2x + 0.7y = 25$$

$$x + y = 50$$

c. Solve the system algebraically.

$$x = 50 - y$$

$$0.2(50-y) + 0.7y = 25$$

$$x = 50 - 30$$

$$10 - 0.2y + 0.7y = 25$$

$$x = 20$$

$$\frac{0.5y}{0.5} = \frac{15}{0.5}$$

$$y = 30$$

20lb of 20% gold

30lb of 70% gold