

Just Bits

- Inside the computer, all information is stored as **bits**
 - A “bit” is a single unit of information
 - Each “bit” is set to either zero or one
- How do we get complex systems like Google, Matlab, and our cell phone apps?

1 0

interpreter

Abstraction!

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

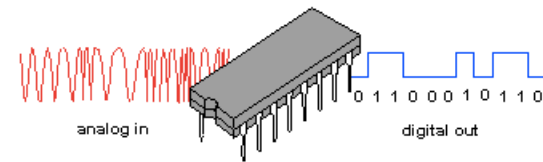
Language: I will use my words to explain my addition and calculation process to others in the class.

What's a Bit Between Friends?

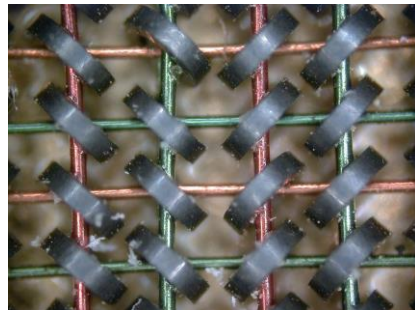
- Bits can be represented in *many* different ways
- They are all equivalent *abstractions*



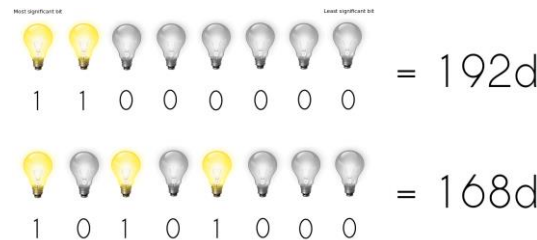
From Computer Desktop Encyclopedia
© 1998 The Computer Language Co. Inc.



Electrical voltages
babbage.cs.qc.edu



Magnetic core memory
(each core represents one bit)
wikipedia.com



Light signals
delightlylinux.files.wordpress.com

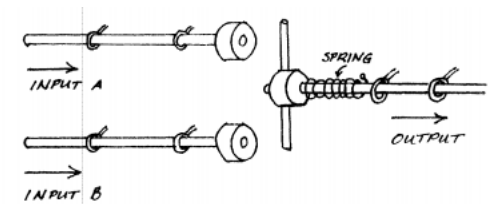


FIGURE 4
Mechanical implementation of the OR function

Mechanical devices
Hillis, *The Pattern on the Stone*

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

The Jacquard Loom



Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Storing Bits



- How are these “bits” stored in modern computers?
- A bit is just an electrical signal or voltage
(by convention: “low voltage” = 0; “high voltage” = 1)
- A circuit called a “flip-flop” can store a single bit
 - A flip-flop can be “set” (using an electrical signal) to either 0 or 1
 - The flip-flop will hold that value until it receives a new signal telling it to change
- Bits can be operated on using **gates** (which “compute” a function of two or more bits)

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Orders of Magnitude

- One $0/1$ ² (“no/yes”) “bit” is the basic unit of memory
 - Eight (2^3) bits = one byte
 - 1,024 (2^{10}) bytes = one kilobyte (1K)*
 - 1,024K = 1,048,576 (2^{20} bytes) = one megabyte (1M)
 - 1,024K (2^{30} bytes) = one gigabyte (1G)
 - 1,024 (2^{40} bytes) = one terabyte (1T)
 - 1,024 (2^{50} bytes) = one petabyte (1P)
 - ... 2^{80} bytes = one yottabyte (1Y?)

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Scaling Up Memory

- Computer **chip**:
 - Many (millions) of circuits
 - Etched onto a silicon wafer using VLSI (Very Large-Scale Integration) technology
 - Lots of flip-flops or DRAM devices == memory chip

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Scaling Up Memory

- Each byte has an **address** (and we use binary numbers to represent those addresses...)
 - An address is represented using a **word**, which is typically either;
 - 2 bytes (16 bits) -- earliest PCs
 - Only 64K combinations \Rightarrow memory is limited to 64K (65,535) bytes!
 - 4 bytes (32 bits) -- first Pentium chips
 - This brings us up to 4G (4,294,967,295) bytes of memory!
 - 8 bytes (64 bits) -- modern Pentium chips
 - Up to 16.8 *million terabytes* (that's 18,446,744,073,709,551,615 bytes!)

Objectives:

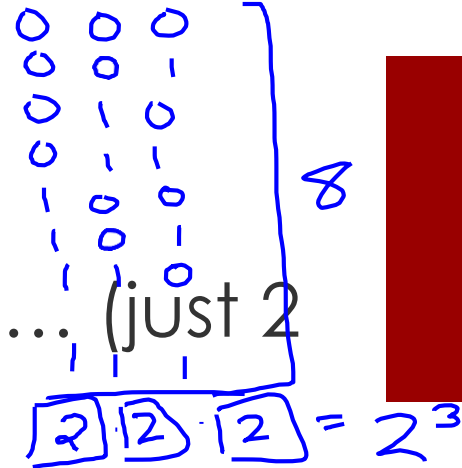
Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Storing Information

- One bit can't tell you much... (just 2 possible values)



- Usually we group 8 bits together into one "byte"

- **QUESTION: How many possible values (combinations) are there for one byte?**

$$2 \cdot 2 \cdot 2 \cdot 2$$
$$2^4$$

$$1 = 2$$
$$2 = 4$$
$$3 = 8$$
$$4 = 2^4 = 16$$

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Storing Information



- A byte can just be thought of as an 8-digit binary (base 2) number
 - [Michael Littman's octopus counting video](#) [3 min]
- Low-order or least significant bit == ones place
 - Next bit would be “10s place” in base 10 -- **what about base 2?**
- High-order bit or most significant bite in a byte == **?? place**

!

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Conversions

107

$$\begin{array}{cccc} & 1 & 1 & 0 & 1 \\ \rightarrow & 2^3 & 2^2 & 2^1 & 2^0 \\ 8 & + & 4 & + & 0 & + & 1 \\ - & - & - & - & - \end{array}$$



- Binary \rightarrow decimal: multiply each digit by its place value and add the results

- Decimal \rightarrow binary: 01101011



- Find the largest power of two that is less than or equal to the decimal number

10

15

- Put a one in that place column in the binary number

$2^4 - 1$

- Add spaces for the smaller binary digits

- E.g., if the largest multiple of two that fits is 256, you would write:

20

1 _ _ _ _ _

- Find the next smallest multiple of two
- Put a one in that place column (and a zero in any columns you skipped)

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Conversions

- **EXERCISE:** You try it!
 - Write ~~3~~97₁₀ in binary

$$\begin{array}{r} 97 \\ - 64 \\ \hline 33 \end{array}$$

$$128 \quad 01100001$$

$$2^8 - 1 = 255$$

- Write 11001110₂ in decimal

$$\begin{array}{c} \uparrow \quad \uparrow \\ 2^1 \quad 2^0 \end{array}$$



Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Practice with Binary



Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.

Homework



DECIMAL TO BINARY

41	
30	
5	
10	
99	
123	
244	
13	
78	
143	
94	
58	
190	
202	
6	

BINARY TO DECIMAL

1111	
1101	
100101	
10	
00111100	
100	
110	
11111101	
1000100	
100001	
11010	
10101011	
10011001	
1110111	
11111	

Objectives:

Content: I will be able to work with numbers from different numbering systems.

Social: I will explain my reasoning to other people.

Language: I will use my words to explain my addition and calculation process to others in the class.